

Association of oxygen vacancies with impurity metal ions in lead titanatePaul Erhart,^{1,2} Rüdiger-Albert Eichel,³ Petra Träskelin,^{4,5} and Karsten Albe¹¹*Institut für Materialwissenschaft, Technische Universität Darmstadt, 64287 Darmstadt, Germany*²*Chemistry, Materials and Life Sciences Directorate, Lawrence Livermore National Laboratory, Livermore, California 94551, USA*³*Eduard-Zintl-Institut, Technische Universität Darmstadt, 64287 Darmstadt, Germany*⁴*Accelerator Laboratory, University of Helsinki, 00014 Helsinki, Finland*⁵*Department of Chemical Engineering and Materials Science, University of California at Davis, Davis, California 95616, USA*

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Thermodynamic, structural, and electronic properties of isolated copper and iron atoms as well as their complexes with oxygen vacancies in tetragonal lead titanate are investigated by means of first principles calculations. Both dopants exhibit a strong chemical driving force for the formation of $M_{\text{Ti}}-V_{\text{O}}$ ($M=\text{Cu,Fe}$) defect associates. The most stable configurations correspond to a local dipole aligned along the tetragonal axis parallel to the spontaneous polarization. Local spin moments are obtained and the calculated spin densities are discussed. The calculations provide a simple and consistent explanation for the experimental findings. The results are discussed in the context of models for degradation of ferroelectric materials.

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I. INTRODUCTION

Piezoelectric materials transform electric signals into mechanical response and vice versa. They are widely used in sensors and actuators as well as in nonvolatile memory devices. The properties of piezoelectrics and their behavior in the presence of electric fields are intimately linked to the defect structures (point defects, domain walls, and grain boundaries) present in these materials.

Defect dipoles, for instance, formed by the association of oxygen vacancies with metal impurities affect the switching behavior as well as aging and fatigue of piezoelectric materials.¹ Their existence has been shown both experimentally¹⁻⁴ and theoretically.⁵ However, a comprehensive microscopic picture of the electronic, structural, and kinetic properties of these defect associates is still lacking. Such detailed knowledge is, however, a prerequisite for understanding electrical “aging” and ferroelectric “fatigue” as exemplified by the model by Arlt and Neumann,^{6,7} which relates these macroscopic degradation phenomena to microscopic processes. Since the time the first phenomenological models were developed,^{6,7} quantum mechanical methods have become available which are both efficient and sufficiently reliable for assessing the energetics of point defect and associates, directly. In the past, several studies addressed the properties of intrinsic point defects with particular attention to oxygen vacancies.⁸⁻¹³ The role of dopants and impurities and the formation of defect dipoles has also been elucidated,^{3-5,14} but important aspects such as the dependence of the formation energies on the Fermi level and the charge state have not been investigated in sufficient detail. Also, a comparative study of the different possible metal impurity-oxygen vacancy configurations, which could serve as input for the defect models referenced above, is not available yet. Such information is, however, crucial both for understanding the generic properties of different impurities and/or dopants and for identifying properties which differentiate them, in particular, with regard to their effect on aging and fatigue. These considerations motivate the present work,

in which density functional theory calculations are employed to study the energy surface for unbound oxygen vacancies and oxygen vacancies complexed with Fe or Cu impurities in tetragonal lead titanate. The results are discussed in the context of existing defect models and have been used to interpret recent electron spin resonance experiments.¹⁵

II. METHODOLOGY**A. Computational details**

Quantum mechanical calculations based on density functional theory (DFT) were carried out using the Vienna *ab initio* simulation package (VASP) which implements the pseudopotential-plane wave approach.¹⁶⁻¹⁹ The projector-augmented wave method was employed for representing the ionic cores and core electrons.^{20,21} In accord with earlier calculations (see, e.g., Refs. 8 and 4), the 5*d* electrons of Pb and the 3*s* and 3*p* electrons of Ti were treated as semicore states, while for Cu and Fe, the valence configuration included the 4*d*, 3*d*, and 3*p* electrons. All calculations were performed using Gaussian smearing with a width of $\sigma=0.2$ eV and a $4\times 4\times 4$ Monkhorst-Pack mesh for Brillouin zone sampling.²² Calculations were carried out using the local spin density approximation (LSDA) to account for the magnetic behavior of iron.⁵⁰ Some calculations were also repeated using the nonspin polarized local density approximation (LDA). The difference between the LDA and LSDA results allows us to estimate the spin contribution for a particular defect or charge state.

With this computational setup, we obtain a lattice constant of $a_0=3.866$ Å and an axial ratio of $c/a=1.05$ for the tetragonal phase of PbTiO₃ in reasonable agreement with experiment. The calculated band gap of 1.47 eV is considerably smaller than the experimental value but consistent with the well known LSDA band gap error. Since there is no unique procedure for correcting the band gap error (see, e.g., Refs. 23-25), in the present work, we abstain from any explicit corrections and discuss the electronic transition levels relative to

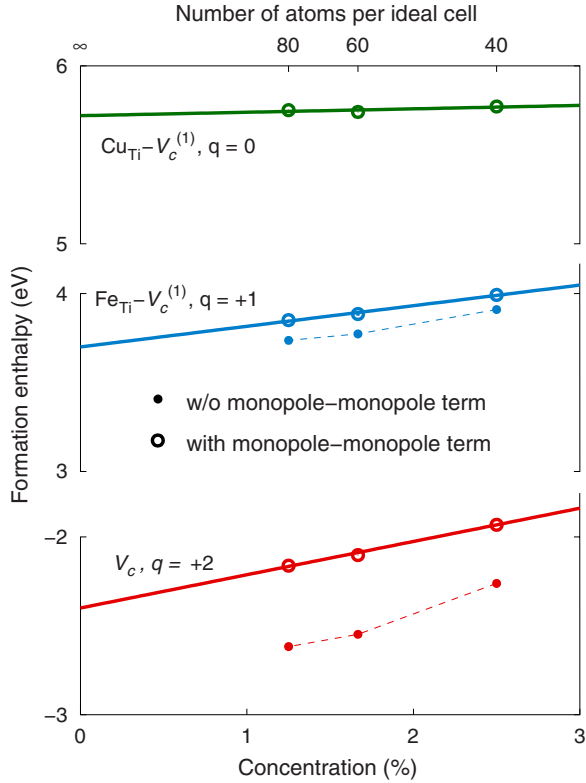


FIG. 1. (Color online) Finite-size scaling of formation enthalpies to obtain formation energies in the limit of infinite dilution for three of the most important defects. The small filled and large open circles show the data before and after application of the monopole-monopole correction term.

the calculated band edges instead (see also our discussion in Sec. III A).

In order to model the defect configurations, supercells containing $2 \times 2 \times 2$ to $2 \times 2 \times 4$ unit cells equivalent to 40–80 atoms were employed. Each configuration was relaxed until the maximum force was less than $15 \text{ meV}/\text{\AA}$. For charged defects, a homogeneous background charge was added. Finite-size scaling was employed in order to obtain the formation and binding energies at infinite dilution.^{26,27} For the charged defect calculations, monopole-monopole interactions were explicitly corrected^{26,28} using values of $\epsilon_{11}^S = 100$ and $\epsilon_{33}^S = 34$ for the static dielectric tensor,⁵¹ while higher order terms were implicitly included by the finite-size scaling procedure.^{26,27} Both the effects of the monopole-monopole term and the finite-size procedure are illustrated in Fig. 1 for three of the most important defects which demonstrates that the finite-size scaling approach works reliably in the present case. The extrapolation errors of the finite-size scaling procedure are given in Tables I–III. These values are a measure for the quality of the finite-size scaling procedure only, and do not include other errors intrinsic to DFT.

B. Formation energies

The formation energy of an intrinsic defect in charge state q depends on the relative chemical potentials of the constitu-

TABLE I. Formation energies (eV) for unbound oxygen vacancies in tetragonal lead titanate for a Fermi level at the valence band maximum ($\mu_e = 0 \text{ eV}$) and metal-rich conditions ($\Delta\mu_{\text{Pb}} = \Delta\mu_{\text{Ti}} = 0 \text{ eV}$). The finite-size scaling extrapolation errors are given in parentheses in the last column.

Defect		40	60	80	Extrapolated	
V_{ab}	0	0.96	0.95	0.95	0.95	(<0.01)
	+1	-0.40	-0.43	-0.43	-0.47	(0.01)
	+2	-1.64	-1.62	-1.62	-1.60	(<0.01)
V_c	0	1.07	0.87	0.70	0.35	0.08
	+1	-0.59	-0.88	-0.96	-1.35	0.06
	+2	-1.93	-2.10	-2.16	-2.40	0.03

ents, $\Delta\mu_i$, and the Fermi level (electron chemical potential) μ_e according to^{29,30}

$$\Delta E_D^f = (E_D - E_H) + q(E_{\text{VBM}} + \mu_e) - \sum_i \Delta n_i (\mu_i^{\text{bulk}} + \Delta\mu_i), \quad (1)$$

where E_D is the total energy of the defective system, E_H is the total energy of the perfect reference cell, E_{VBM} is the position of the valence band maximum, Δn_i denotes the difference between the number of atoms of type i in the reference cell with respect to the defective cell, and μ_i^{bulk} is the chemical potential of the reference phase of atom type i . In the present context, we are not concerned with the effect of the chemical environment [$\Delta\mu_i$ in Eq. (1)] but focus on the transition levels and the binding energies between oxygen vacancies and metal impurities and/or dopants [see Eq. (2) below], both of which are independent of the chemical potentials.

The binding energy for the metal impurity-oxygen vacancy ($M_{\text{Ti}} - V_{\text{O}}$) associates considered below is calculated as the difference between the formation energies of the defect, complex and the isolated defects,

$$E_b = \Delta E_D^f[M_{\text{Ti}} - V_{\text{O}}] - \Delta E_D^f[M_{\text{Ti}}] - \Delta E_D^f[V_{\text{O}}]. \quad (2)$$

The binding energy depends on the Fermi level due to the Fermi level dependence of the formation energies. For a given value of μ_e , the difference in Eq. (2) is calculated between the most stable charge states for each defect involved. By insertion of Eq. (1) into Eq. (2), one can show that the terms with Δn_i cancel, whence E_b is independent of the chemical potentials, $\Delta\mu_i$. Following the sign convention introduced via Eq. (2), negative values for E_b imply that the system gains energy by association, whereas positive values imply an effective repulsion between the isolated defects.

III. RESULTS

A. Isolated oxygen vacancies

The crystallographic structure of a tetragonal perovskite possesses two symmetrically inequivalent oxygen sites which are located within the ab plane and along the c axis,

TABLE II. Formation energies (LSDA) in units of eV for isolated and complexed Cu impurities on Ti sites (Cu_{Ti}) in tetragonal lead titanate for a Fermi level at the valence band maximum ($\mu_e=0$ eV) and metal-rich conditions ($\Delta\mu_{\text{Pb}}=\Delta\mu_{\text{Ti}}=\Delta\mu_{\text{Cu}}=0$ eV). The finite-size scaling extrapolation errors are given in parentheses in the last but one column. $\Delta n_{\uparrow\downarrow}$ denotes the difference between the number of electrons in spin-up and spin-down states.

Defect	$\Delta n_{\uparrow\downarrow}$	40	60	80	Extrapolated	
Cu_{Ti}						
-3		11.81	12.04	12.06	12.35	(0.10)
-2	1	10.16	10.28	10.30	10.46	(0.05)
-1	2	9.74	9.79	9.81	9.88	(0.01)
0		9.97	9.95	10.07	10.11	(0.14)
$\text{Cu}_{\text{Ti}}-V_{ab}$						
-2		9.22	9.32	9.32	9.45	(0.06)
-1	0	7.23	7.36	7.41	7.60	(0.01)
0	1	6.43	6.45	6.48	6.52	(0.02)
+1	0	6.67	6.62	6.60	6.52	(0.01)
$\text{Cu}_{\text{Ti}}-V_c^{(1)}$						
-2		8.83	8.91	8.91	9.01	(0.04)
-1	0	6.86	6.94	6.99	7.11	(0.01)
0	1	5.77	5.74	5.75	5.72	(0.03)
+1	0	6.02	5.94	5.91	5.80	(0.01)
$\text{Cu}_{\text{Ti}}-V_c^{(2)}$						
-2		9.33	9.57	9.69	10.04	(<0.01)
-1	0	7.29	7.59	7.77	8.24	(0.03)
0	1	6.22	6.43	6.59	6.93	(0.06)
+1		6.44	6.64	6.80	7.14	(0.07)
$\text{Cu}_{\text{Ti}}-V_c^{(3)}$						
-2			10.00	10.01	10.04	
-1	0		7.98	8.04	8.22	
0	1		6.76	6.75	6.74	
+1			6.97	6.89	6.68	
$\text{Cu}_{\text{Ti}}-V_c^{(4)}$						
-2				10.21		
-1	0			8.26		
0	1			6.98		
+1				7.14		

respectively. Based on DFT calculations, Park and Chadi⁸ identified one possible vacancy configuration along the c axis (V_c) and two distinct vacancies configurations within the ab plane (V_{ab}^{sw} , V_{ab}^{ud}). The latter two configurations differ in the orientation of the polarization above and below the vacancy plane. In the present work, we have found the “up-down” configuration (V_{ab}^{ud} , see Ref. 8 for nomenclature), in which the polarization vectors are oriented head to head in the vacancy plane, to be highly unstable with respect to the “switchable” configuration (V_{ab}^{sw}), which is characterized by a uniform orientation of the polarization vector. Although Park and Chadi did not provide a quantitative energy comparison for V_{ab}^{sw} and V_{ab}^{ud} due to the missing data for the 180° domain wall energy, they estimated the V_{ab}^{sw} configuration to be lower

in energy.⁸ For these reasons, we focus on the V_{ab}^{sw} configuration which for the sake of brevity in the following is denoted by V_{ab} .

Table I summarizes the formation energies for unbound oxygen vacancies obtained for extreme metal-rich conditions ($\Delta\mu_{\text{Pb}}=\Delta\mu_{\text{Ti}}=0$ eV). In all charge states, the c -type vacancy is energetically preferred over the ab -type vacancy in agreement with the calculations in Ref. 8. For infinite dilution (extrapolated values in Table I), the energy difference is as large as 0.8 eV for $q=+2$ which is on the order of magnitude of the energy barrier for migration.³¹

The variation of the formation energy with the Fermi level is shown in Fig. 2. Practically, over the entire band gap, oxygen vacancies are doubly positively charged. For the

TABLE III. Formation energies (LSDA) in units of eV for isolated and complexed Fe impurities on Ti sites (Fe_{Ti}) in tetragonal lead titanate for a Fermi level at the valence band maximum ($\mu_e=0$ eV) and metal-rich conditions ($\Delta\mu_{\text{pb}}=\Delta\mu_{\text{Ti}}=\Delta\mu_{\text{Fc}}=0$ eV). The finite-size scaling extrapolation errors are given in parentheses in the last but one column. $\Delta n_{\uparrow\downarrow}$ denotes the difference between the number of electrons in spin-up and spin-down states. The difference between electrons in spin-up and spin-down states $\Delta n_{\uparrow\downarrow}$ for the configuration with the lowest energy is system size dependent.

Defect	$\Delta n_{\uparrow\downarrow}$	40	60	80	Extrapolated	
Fe_{Ti}						
-2	0	8.64	8.81	8.87	9.11	(0.04)
-1	1	7.14	7.18	7.21	7.27	(<0.01)
0	2	6.26	6.23	6.23	6.19	(0.01)
+1	3	6.15	6.12	6.10	6.05	(<0.01)
$\text{Fe}_{\text{Ti}}-V_{ab}$						
-2	0	8.69	8.91	8.96	9.25	(0.07)
-1	1	6.94	6.99	7.01	7.08	(<0.01)
0	2	5.46	5.44	5.44	5.41	(0.02)
+1	3	4.49	4.43	4.40	4.31	(<0.01)
+2	4	4.18	4.14	4.09	4.01	(0.04)
$\text{Fe}_{\text{Ti}}-V_c^{(1)}$						
-2	0	8.42	8.52	8.53	8.65	(0.05)
-1	1	6.50	6.52	6.53	6.56	(<0.01)
0	2	5.00	4.93	4.93	4.84	(0.04)
+1	3	3.99	3.88	3.85	3.70	(0.02)
+2	4	3.82	3.73	3.68	3.54	(0.02)
$\text{Fe}_{\text{Ti}}-V_c^{(2)}$						
-2	0	8.61	9.08	9.43	10.20	(0.13)
-1	1	6.83	7.17	7.39	7.92	(0.06)
0		5.40	5.60	5.46	5.62	(0.27)
+1		4.34	4.25	4.25	4.15	(0.05)
+2	4	4.09	4.16	4.17	4.25	(0.03)
$\text{Fe}_{\text{Ti}}-V_c^{(3)}$						
-2	0		9.19	9.11	8.86	
-1	0		6.97	6.87	6.55	
0	0		5.26	5.21	5.07	
+1	1		4.32	4.23	3.96	
+2	2		4.24	4.10	3.69	
$\text{Fe}_{\text{Ti}}-V_c^{(4)}$						
-2	0			9.42		
-1	0			7.21		
0	0			5.55		
+1	1			4.54		
+2	2			4.27		

given chemical conditions, the formation energies are negative which indicates that the material is unstable for these chemical potentials ($\Delta\mu_{\text{pb}}=\Delta\mu_{\text{Ti}}=0$ eV). If the oxygen partial pressure is raised (i.e., $\Delta\mu_{\text{Ti}}$ and $\Delta\mu_{\text{pb}}$ become less negative, while $\Delta\mu_{\text{O}}$ becomes more negative), the oxygen vacancy formation energy increases and the stability condition is fulfilled.

On first sight, the present finding is at variance with the calculations in Ref. 11 in which the +2/0 transition level of the oxygen vacancy is located in the middle of the band gap. This finding is, however, a consequence of the corrections applied in that work: In order to correct for the band gap error, the conduction band minimum was rigidly shifted upward *without* correcting the formation energies. If this shift is

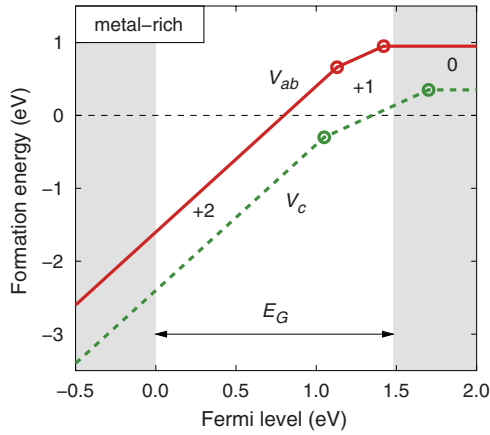


FIG. 2. (Color online) Variation of the formation energy of unbound oxygen vacancies with the Fermi level for extreme metal-rich conditions ($\Delta\mu_{\text{Pb}}=\Delta\mu_{\text{Ti}}=0$ eV). The white area corresponds to the calculated band gap. The numbers indicate the defect charge state.

omitted, the results of Ref. 11 and the findings of the present work are consistent with each other. The approach in Ref. 11 ignores the fact that in the case of singly charged (V_{O}^{\bullet}) and neutral oxygen vacancies (V_{O}^{\times}), the excess electron(s) occupies the conduction band states. In order to maintain internal consistency, a correction term²³ on the order of $z_e\Delta E_G$ would have to be added to the formation energies of V_{O}^{\bullet} and V_{O}^{\times} , where z_e is the number of occupied conduction band states and ΔE_G denotes the difference between the calculated and the experimental band gap.⁵² If these energy terms are included, the +2/+1 (+2/0) transition is no longer located in the middle of the (experimental) band gap but near the conduction band minimum. This is equivalent to the location of the transition level with respect to the calculated conduction band minimum (CBM) if no correction is applied.

1. Isolated copper impurities

Since there is experimental evidence that copper impurities in lead titanate preferentially occupy Ti sites,³²⁻³⁴ only the substitutional position was considered (Cu_{Ti}) in the present calculations. The calculated formation energies for different charge states of Cu_{Ti} are compiled in Table II for extreme metal-rich conditions ($\Delta\mu_{\text{Pb}}=\Delta\mu_{\text{Ti}}=\Delta\mu_{\text{Cu}}=\Delta\mu_{\text{Fe}}=0$ eV). They can be used to derive the Fermi level dependence of the defect formation energy, as demonstrated in Fig. 3 which shows that uncomplexed Cu impurities can occur in charge states $q=-1$ and -2 . The transition between these two charge states is located ~ 0.2 eV below the middle of the calculated band gap.

In the defect chemistry of oxides, often a fully ionic picture is adopted, e.g., in Cu-doped lead titanate Cu^{2+} ions are usually assumed to replace Ti^{4+} ions with two defect electrons being associated with the defect site. In Kröger-Vink notation the resulting defect is written as Cu_{Ti}'' . Accordingly, copper impurities should act as acceptors and create holes in the valence band.

The present quantum-mechanical calculations are free of

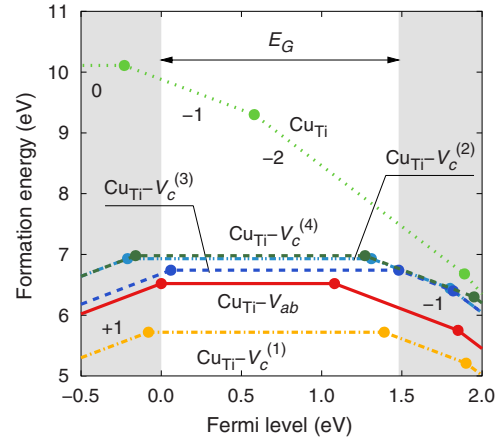


FIG. 3. (Color online) Fermi level dependence of formation energies of free and complexed Cu impurities. Parallel lines imply equal charge states as indicated in the plot. The white stripe indicates the (calculated) band gap while the gray stripes indicate the valence and conduction bands, respectively. Extrapolated formation energies from Table II were used except for $\text{Cu}_{\text{Ti}}-V_c^{(4)}$ for which the data obtained with 80-atom cells are shown.

a priori assumptions with respect to the oxidation state of a defect: Different charge states q are obtained by varying the number of electrons in the *entire* system. In order to provide a connection between the ionic picture outlined above and the charge states given in Table II and Fig. 3, one must therefore analyze the electronic structure of the defect.

The partial and total densities of states for a neutral ($q=0$) copper impurity in comparison with the ideal (defect-free) system are shown in Fig. 4. The bottom of the conduction band is predominantly composed of Ti 3d orbitals (feature A in Fig. 4). Since in this energy range the contribution Cu 3d orbitals is practically zero, copper substitution leads to

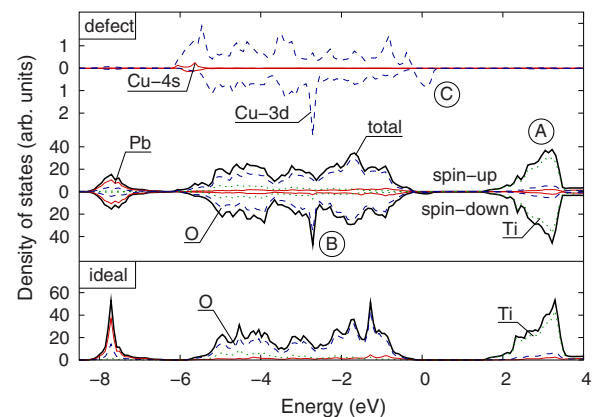


FIG. 4. (Color online) Spin-decomposed total and partial densities of states for neutral uncomplexed Cu impurities in lead titanate. The partial densities of states for the Cu atom have been scaled by a factor of 20 and are shown separately in the upper part of the figure. The density of states for the ideal crystal is shown below. In the latter case, the density of states is independent of the spin orientation. A Gaussian filter with $\sigma=0.05$ eV was applied to optimize the visualization.

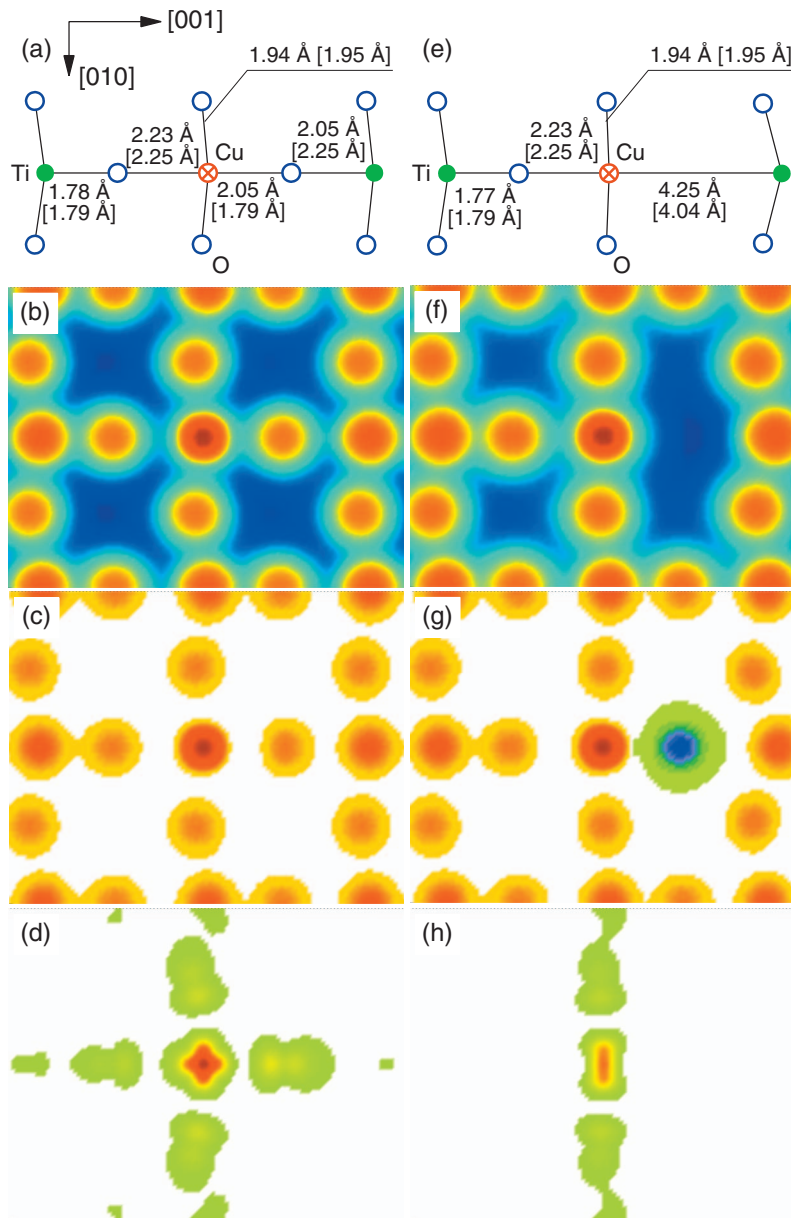


FIG. 5. (Color) [(a)–(d)] Isolated copper impurity in charge state $q = -1$ and [(e)–(h)] copper impurity-oxygen-vacancy complex in charge state $q = 0$. [(a) and (e)] Position of atoms in the (100) plane containing the defect; numbers given in brackets give the equivalent distances in the defect-free crystal. [(b) and (f)] Total charge density; a logarithmic scale has been chosen for the charge density in order to enhance the features. [(c) and (g)] Difference between total charge density of defective cell and defect-free cell. [(d) and (h)] Spin densities.

an effective reduction of the density of states at the bottom of the conduction band. With regard to the top of the valence band, the most obvious feature is a hybridization of Cu $3d$ orbitals with O $2p$ orbitals (feature B in Fig. 4), while the contribution of Cu $4s$ and Cu $3p$ states is negligible. In addition, a Cu-induced state emerges attached to the valence band edge (feature C in Fig. 4). As electrons are added to the system, this defect induced state is, however, shifted into the band gap because the excess charge is localized in a small volume around the defect. As a result, the local potential at the copper atom is modified and an energy offset of the electronic states of this defect is induced.

Integrating the density of states and the occupied levels up to the valence band edge and including the defect induced

peak reveals three empty levels (holes) for the neutral charge state. As electrons are added to the system ($q < 0$), these empty states are gradually filled. For the charge state -1 , there are two holes localized at the Cu atom. The situation is thus equivalent to placing a Cu^{2+} on a Ti site giving $\text{Cu}_{\text{Ti}}^{2+}$, while for $q = -2$, there is one unoccupied valence band level corresponding to $\text{Cu}_{\text{Ti}}^{3+}$ (Cu^+ on Ti^{4+}). If the Fermi level is located in the middle of the band gap, the most stable defect is $\text{Cu}_{\text{Ti}}^{3+}$.

The $-1/-2$ transition can be understood as a local reduction of copper: The transition from charge state $q = -1$ to $q = -2$ is equivalent to the reaction $\text{Cu}^{2+} + e^- \rightarrow \text{Cu}^+$. Experimentally, the redox potential for this reaction has been measured in aqueous solution to be $+0.16$ eV with respect to the

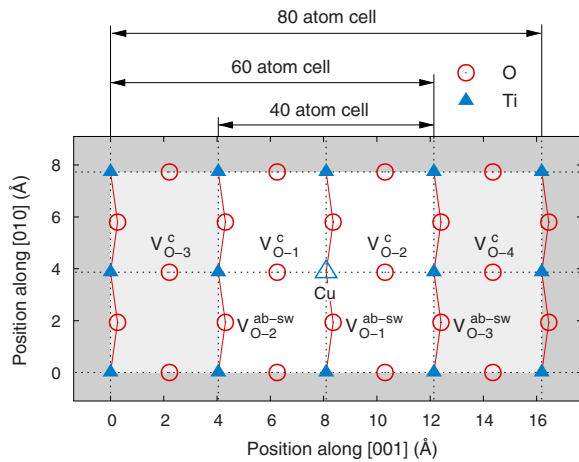


FIG. 6. (Color online) Schematic of different conceivable vacancy-impurity atom configurations. The tetragonal perovskite lattice is shown along the [100] axis and Pb atoms have been omitted for clarity. The different gray shaded areas indicate the size of the different supercells employed in the present work.

standard hydrogen electrode, which on an absolute energy scale is located at 4.5 eV.³⁵ Thus, the $\text{Cu}^{++}/\text{Cu}^+$ redox potential is 4.7 eV. On the other hand, the electron affinity of PbTiO_3 is 3.5 eV and the band gap is about 3.4 eV (Ref. 36 and references therein) placing the valence band maximum (VBM) 6.9 eV below the vacuum level. In analogy, the redox reaction occurs roughly in the middle of the band gap (1.2 eV below the CBM or 2.2 eV above the VBM), which is in good agreement with the present calculations which locate the $-1/-2$ (or $\text{Cu}^{++}/\text{Cu}^+$) transition level near the midgap. This analogy has, however, merely a qualitative character.

In order to obtain a measure for the spin polarization of copper defects, we calculated the difference between the number of electrons in spin-up and spin-down states ($\Delta n_{\uparrow\downarrow}$ in Table II). In both relevant charge states ($q=-1$ and -2), unpaired electrons are present in the system which allows us to probe the defect center spectroscopically.

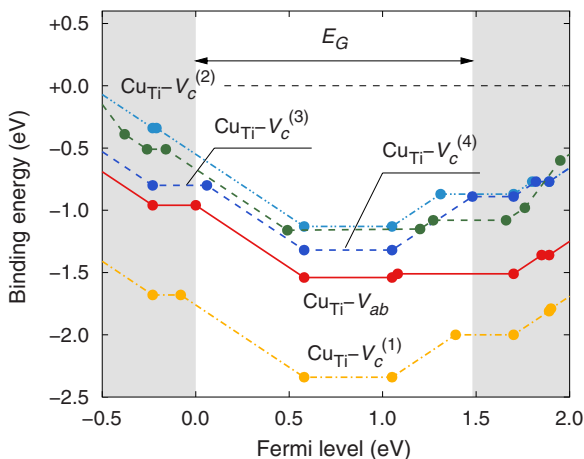


FIG. 7. (Color online) Binding energies for Cu impurities in tetragonal lead titanate obtained from the extrapolated formation energies given in Tables I and II. Negative energies imply a chemical driving force for association.

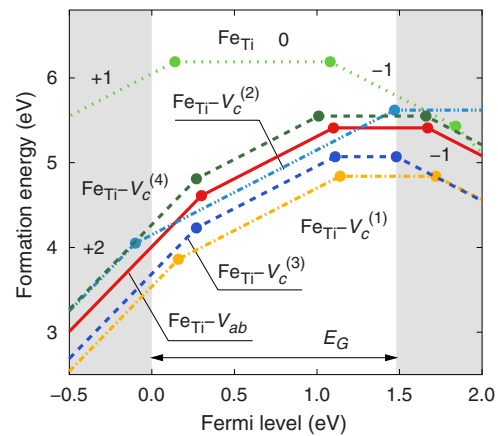


FIG. 8. (Color online) Fermi level dependence of formation energies of free and complexed Fe impurities. Parallel lines imply equal charge states as indicated in the plot. The white stripe indicates the (calculated) band gap, while the gray stripes indicate the valence and conduction bands, respectively. Extrapolated formation energies from Table III were used except for $\text{Fe}_{\text{Ti}}-\text{V}_c^{(4)}$ for which the data obtained with 80-atom cells are shown.

The geometry and charge density of an isolated copper impurity in charge state $q=-1$ are shown in Fig. 5. In comparison with the ideal crystal, copper substitution causes the B site to move toward the oxygen (100) plane. For the charge state $q=-1$ ($q=-2$), the relative displacement of the copper atom with respect to its in-plane oxygen neighbors is 0.15 Å (0.19 Å) along [001], compared to 0.28 Å in the defect-free crystal. Copper substitution thus causes a relaxation of the B-site atom in the direction of the nearest oxygen plane. The charge density plots show that the defect charge [Fig. 5(c)] as well as the spin asymmetry [Fig. 5(d), also compare Fig. 4]

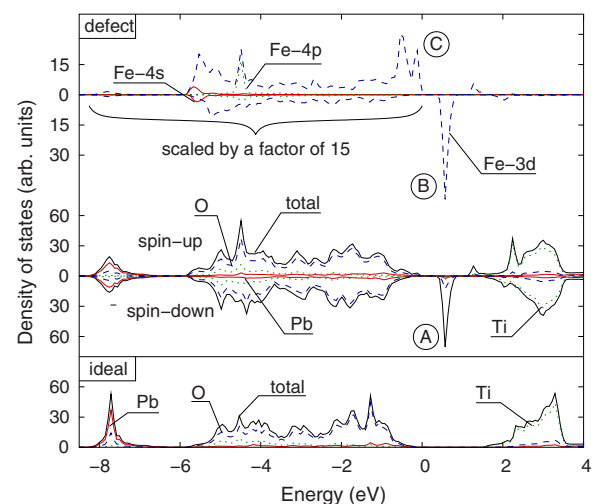


FIG. 9. (Color online) Spin-decomposed total and partial densities of states for neutral uncomplexed Fe impurities in lead titanate. The partial densities of states for the Fe d orbitals are shown separately in the upper part of the figure. The Fe s and Fe p states have been omitted since in the energy window shown they are practically zero. A Gaussian filter with $\sigma=0.05$ eV was employed to smoothen the data.

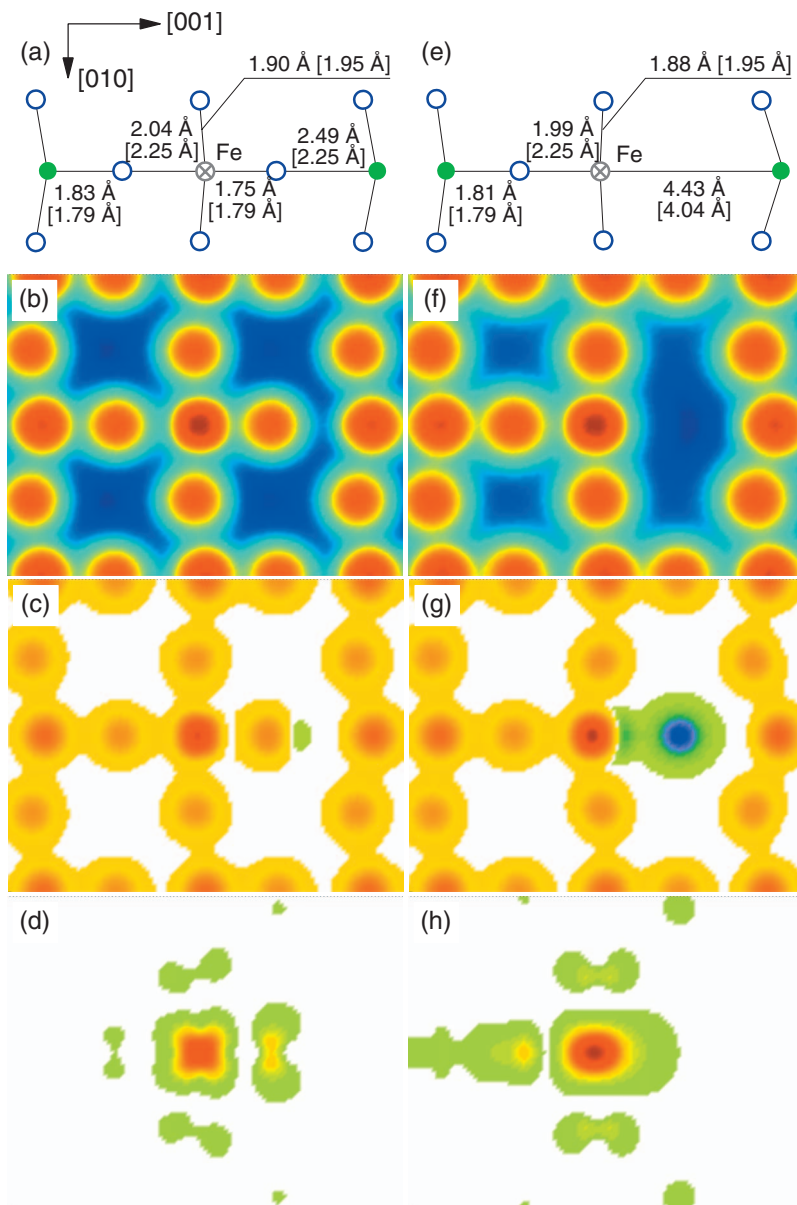


FIG. 10. (Color) [(a)–(d)] Isolated iron impurity in charge state $q=0$ and [(e)–(h)] iron impurity-oxygen-vacancy complex in charge state $q=+1$. [(a) and (e)] Position of atoms in the (100) plane containing the defect; numbers given in brackets give the equivalent distances in the defect-free crystal. [(b) and (f)] Total charge density; a logarithmic scale has been chosen for the charge density in order to enhance the features. [(c) and (g)] Difference between total charge density of defective cell and defect-free cell. [(d) and (h)] Spin densities.

are localized at the copper atom. In addition, the difference between the spin densities in the (100) plane reveals a slight asymmetry with respect to the tetragonal axis. Analysis of the electron and spin density at farther atoms—in particular, the nearest Pb atoms in the (110) plane—indicates that both of them are virtually unaffected by the presence of the Cu impurity.

2. Copper-vacancy complexes

As illustrated in Fig. 6, different configurations for defect associates of oxygen vacancies with B -site impurities are conceivable. Since the impurity atom breaks the translational symmetry along the c axis, the degeneracy of the positions above and below the impurity atom is lifted. In the first

neighbor shell, one can distinguish configurations in which the oxygen vacancy is placed along the c axis either below ($M_{\text{Ti}}-V_c^{(1)}$, shorter $M_{\text{Ti}}-\text{O}$ distance) or above the impurity atom ($M_{\text{Ti}}-V_c^{(2)}$, longer $M_{\text{Ti}}-\text{O}$ distance), or on one of the four symmetry equivalent sites within the ab plane ($M_{\text{Ti}}-V_{ab}$). If one considers the second-nearest neighbor shell, another two configurations involving c -type vacancies are possible ($M_{\text{Ti}}-V_c^{(3)}$, $M_{\text{Ti}}-V_c^{(4)}$). Further configurations are obtained by placing the vacancy on second-nearest neighbor ab sites (e.g., $M_{\text{Ti}}-V_{ab}^{(2)}$ and $M_{\text{Ti}}-V_{ab}^{(3)}$ in Fig. 6). In the present work, we have considered first- and second-nearest neighbor configurations involving c -type vacancies as well as first-nearest neighbor configurations with ab vacancies. Exploratory calculations were also carried out for second-

nearest neighbor *ab*-type vacancy associates. This possibility was, however, not pursued further, since the total energies were significantly larger than for the respective lowest energy configuration.

The $\text{Cu}_{\text{Ti}}-V_c^{(1)}$ complex, in which the vacancy is located at the nearest oxygen site along the *c* axis (compare Figs. 6 and 5), is the most stable configuration. The most stable charge state is $q=0$ as expected if one combines $V_{\text{O}}^{\bullet\bullet}$ (see Fig. 2) and Cu_{Ti}'' . The energy difference with respect to the less stable complexes ($[\text{Cu}_{\text{Ti}}-V_{ab}]^{\times}$ and $[\text{Cu}_{\text{Ti}}-V_c^{(3)}]^{\times}$) is rather large (0.8–1.0 eV). This large energy difference is particularly noteworthy since previous model calculations assumed a much smaller energy difference on the order of 0.06 eV (compare Ref. 7).

It is very instructive to compare the charge densities for isolated and complexed copper impurities. As shown in Fig. 5(d), the spin density for the isolated copper impurity is symmetric with respect to fourfold rotations about the [001] axis. This symmetry also applies for the copper-vacancy complex [Fig. 5(h)], but, in addition, the spin density pattern contains a (001) mirror plane through the Cu site. As can be seen by comparison of Figs. 5(a) and 5(e), this distinction results from the shift of the Cu atom which in the presence of a vacancy on the nearest O site relaxes almost completely into the (001) plane of oxygen atoms, leading to a local pseudocubic environment. These observations have important implications for the interpretation of electron paramagnetic resonance measurements, as discussed in Ref. 15.

Finally, one can use the formation energies of isolated oxygen vacancies, copper impurities, and their complexes to derive the binding energy and its dependence on the Fermi level. As shown in Fig. 7, there is a very strong chemical driving force for association of copper impurities with oxygen vacancies irrespective of the Fermi levels. If there are more oxygen vacancies than copper impurities in the system, all copper impurities will be complexed. In the opposite scenario, all oxygen vacancies would be complexed and the number of isolated copper impurities would be reduced by the number of metal impurity-oxygen vacancy associates.

3. Iron impurities

The formation energies for uncomplexed Fe impurities are compiled in Table III and presented as a function of the Fermi level in Fig. 8. The uncomplexed iron impurity occurs predominantly in the neutral charge state ($q=0$). Transition levels are only present near the band edges. It is noteworthy that according to Fig. 8, uncomplexed Fe should display ambipolar behavior. Analysis of the total and partial density of states shows that iron induces a defect level which for the neutral charge state is located in the middle of the band gap (feature A in Fig. 9). The density of states for the two different spin orientations differs considerably. While one spin orientation (spin down in Fig. 9) gives rise to a level in the band gap (feature B in Fig. 9), the other one leads to additional states at the top of the valence band (feature C in Fig. 9). As in the case of copper, strong hybridization occurs between the impurity atom *3d* orbitals and the O *2p* levels of the host material. Also, in equivalence to copper, Fe *3d* levels do practically not contribute to the conduction band, slightly

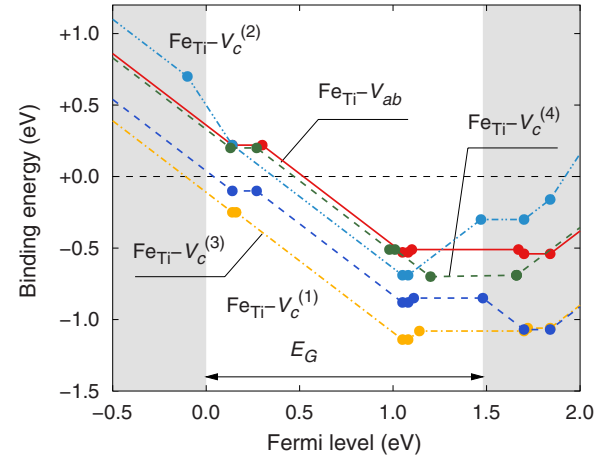


FIG. 11. (Color online) Binding energies as defined by Eq. (2) for Fe impurities in tetragonal lead titanate obtained from the extrapolated formation energies given in Tables I and III. Negative energies imply a chemical driving force for association.

diminishing the density of states at the bottom of this band. Due to the presence of gap states defect induced holes and electrons cannot be unambiguously identified. In contrast to copper, a simple correlation between the Kröger-Vink notation for defects and the charge states q is, therefore, not possible.

The potentials for the redox reactions $\text{Fe}^{3+} + e^- \rightarrow \text{Fe}^{2+}$ and $\text{Fe}^{2+} + 2e^- \rightarrow \text{Fe}^0$ have been measured in aqueous solution to be 0.77 and -0.41 eV, respectively. Based on these values and using the data for the electron affinity and the band gap cited above, one would expect transition levels at 1.6 eV ($\text{Fe}^{3+}/\text{Fe}^{2+}$, i.e., $\text{Fe}_{\text{Ti}}'/\text{Fe}_{\text{Ti}}''$) and 2.8 eV ($\text{Fe}^{2+}/\text{Fe}^0$, i.e., $\text{Fe}_{\text{Ti}}''/\text{Fe}_{\text{Ti}}^{4'}$) with respect to the experimental valence band maximum. In contrast, the present calculations indicate transitions about 0.15 eV above the VBM and 0.39 eV below the CBM. The analogy with the behavior of ions in solution, which worked reasonably in the case of copper, thus appears to fail for iron.

4. Iron-vacancy complexes

The iron-vacancy complexes are analogous to the copper-vacancy associates described in Sec. III A 2 and Fig. 6. In agreement with earlier calculations,⁴ the configuration with the shortest distance between impurity center and oxygen vacancy ($\text{Fe}_{\text{Ti}}-V_c^{(1)}$) is the most stable (Fig. 8). The energetic ordering of the remaining configurations is, however, somewhat different from the case of copper (Fig. 10). This observation has implications for the migration of oxygen vacancies and is discussed in the context of point defect models in Sec. IV and Ref. 31.

The binding energies for Fe impurities shown in Fig. 11 are in general smaller than for copper and for Fermi levels very close to the valence band the binding energy can even become positive. Nonetheless, for most conditions, there is a rather strong ($\gg k_B T$) driving force for association.

Analysis of the spin density shows that for both isolated and associated iron impurities unpaired electrons are local-

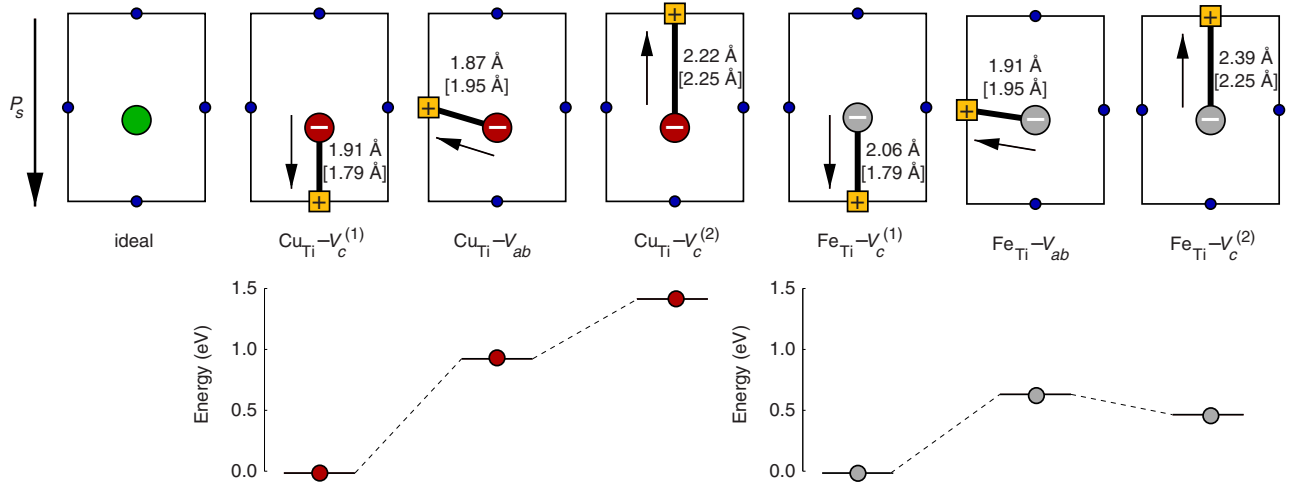


FIG. 12. (Color online) Summary of key results for the most important charge states of nearest neighbor Cu/Fe-vacancy complexes ($[\text{Cu}_{\text{Ti}}-\text{V}_c]^\times$, $[\text{Fe}_{\text{Ti}}-\text{V}_c]^\bullet$). The large arrow on the far left indicates the direction of the spontaneous polarization with respect to the ideal unit cell. The short arrows indicate the direction of the defect induced dipole moments. Distances are given between the impurity atom and the position of the vacancy (as defined by the positions of the neighboring oxygen planes). Values in brackets refer to the ideal (undistorted) lattice. The lower panel visualizes the formation energy differences.

ized in the d -electron states at the iron site (Table III). It furthermore reveals that in both cases the spin density pattern is symmetric with respect to fourfold rotations about the tetragonal axis. Unlike in the case of copper-vacancy associates, the (001) plane is, however, not a mirror plane.

IV. DISCUSSION

The results obtained in this study need to be discussed in the context of degradation phenomena in ferroelectric materials. Two distinct processes have been widely described: (1) The gradual degradation of ferroelectric properties (usually over extended periods of time) in the absence of electric fields is termed “aging.”³⁷ This process is commonly attributed to an increasing restriction of domain-wall motion with time³⁸ and typically accompanied by a shift of the ferroelectric hysteresis loop along the electric field axis.^{39,40} The shift is known as the *internal bias field* and it has been proposed to be related to the relaxation of defect dipoles.^{6,7} In general, acceptor-doped ferroelectric ceramics with high concentrations of oxygen vacancies are particularly prone to aging. (2) The degradation of ferroelectric properties in the presence of a (usually oscillating) electric field is termed electric “fatigue.” There are various contributions to this phenomenon and possible explanations involve defects of all kinds.

The most widely known model for aging^{6,7} relates the appearance of internal bias fields to the existence and gradual reorientation of impurity-oxygen-vacancy defect dipoles. Similar models have been discussed in the literature.^{2,41,42} Experimentally, an increased internal bias field has been observed for aged lead zirconate titanate compounds and was attributed to defect dipole alignment leading to a clamping of domain walls.⁴³

The availability of microscopic information on the energy landscape for defect formation and migration is the key ingredient for these models. The present work provides a

database for these models and allows us to verify their basic assumptions.

The key information regarding the orientation and the magnitude of the defect dipoles as well as their energetic ordering is summarized in Fig. 12. This picture needs to be compared to the energy landscape proposed by Arlt and Neumann^{6,7} on the basis of electrostatic arguments (Fig. 4 in Refs. 6 and 7). The latter analysis was carried out for barium titanate and involved several crucial assumptions with respect to, e.g., the magnitude of the local dipole moment or the dielectric constant in the vicinity of the defect center. In agreement with the conclusions of the Arlt-Neumann model, the quantum-mechanical calculations show that for the energetically most stable configuration ($M_{\text{Ti}}-\text{V}_c^{(1)}$), the defect induced dipole is oriented parallel to the overall spontaneous polarization P_s (compare Fig. 12). Thus in equilibrium (i.e., a state which would be achieved after “infinite” aging), the polarization locally increases due to the formation and alignment of local defect dipoles. In contrast, the defect dipole of the alternative c -axis configuration ($M_{\text{Ti}}-\text{V}_c^{(2)}$) causes a local reduction of the polarization.

In Ref. 7, two estimates for the energy differences between different dipole orientations are derived. The first one treats the defect as a sphere with a defect induced polarization embedded in a ferroelectric matrix. It yields values on the order of 0.5–1.2 eV [compare Eqs. (8a)–(8c) in Ref. 7] which are of a similar magnitude as the values obtained from the present calculations. The second estimate is based on the model of an ideal point dipole and yields much smaller energy differences on the order of 0.03–0.06 eV [Eq. (9) in Ref. 7]. It is important to realize that the modeling of aging carried out in the same paper was actually based on the latter values.

In fact, the energy differences obtained in the present work are actually on the order of magnitude of the barriers for the migration of free oxygen vacancies in this system

(0.8–1.0 eV, see, e.g., Ref. 11). In the vicinity of impurities, the energy surface, which describes the barriers for the transformation of different defect dipole configurations into each other, is therefore severely distorted.³¹ This effect is important for the behavior of defect dipoles in the presence of oscillating electric fields, which pertains to the fatigue of the material.

Finally, Fig. 12 highlights a noteworthy difference between Cu and Fe. While for Cu complexes, the energy difference between $[\text{Cu}_{\text{Ti}}-V_c^{(1)}]^\times$ and $[\text{Cu}_{\text{Ti}}-V_c^{(2)}]^\times$ is as large as 1.21 eV, for $[\text{Fe}_{\text{Ti}}-V_c^{(1)}]^\bullet$ and $[\text{Fe}_{\text{Ti}}-V_c^{(2)}]^\bullet$, the difference is just 0.45 eV. This difference has implications for the redistribution of the defect dipoles in the presence of an oscillating electric field and thus for the process of fatigue. A detailed account of this behavior will be published elsewhere.³¹

V. CONCLUSIONS

This paper presents a comprehensive and detailed investigation of Fe and Cu dopants and/or impurities in tetragonal lead titanate. Both metal ions are found to be very effective traps for oxygen vacancies. In the most stable configurations, the oxygen vacancy is located on a *c* site such that the $M_{\text{Ti}}-V_{\text{O}}$ distance is minimal, and the defect dipole is aligned

parallel the spontaneous polarization. This result is in qualitative agreement with an electrostatic analysis of the defect induced dipole field. An alternative configuration ($M_{\text{Ti}}-V_c^{(2)}$) in which the dipole is oriented antiparallel with respect to the spontaneous polarization is somewhat higher energy but is anticipated to be of importance for the fatigue of lead titanate based ferroelectrics.

Since all relevant defects considered in this investigation carry unpaired electrons, they are visible for electron spectroscopic methods. In fact, by means of analyzing the spin density patterns for different defects, it was possible to interpret recent electron paramagnetic resonance measurements and to resolve an apparent disagreement between experiment and calculations.¹⁵ The results obtained in this study represent important information on the energy landscape for energy formation and association and provide the basis for the improvement of defect models for the degradation of ferroelectric materials.

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⁵⁰While generalized gradient approximations (GGAs) for the exchange-correlation potential give often better agreement with experimental data than the local density approximation, this does not in general apply to ferroelectric perovskites. In the present case, GGAs are observed to overestimate considerably

the equilibrium volume, the axial ratio, as well as the ferroelectric distortion. In particular, for studies of defect properties the LDA is therefore often preferred (see, e.g., Refs. [4,5,8–14]).

⁵¹Ideally, one would obtain the zero-temperature static dielectric tensor from a first principles calculation. To the best of our knowledge, such data are not available for PbTiO_3 , and its determination is a work in its own right (see, e.g., Refs. 44–46). We, therefore, resort here to experimental data. If one extrapolates the temperature dependent data from Ref. 47 to 0 K, one obtains the zero-temperature, clamped dielectric constants $\epsilon_{11}^S = 100$ and $\epsilon_{33}^S = 34$ in reasonable agreement with (room-temperature) measurements (see Refs. 48 and 49 for an overview of experimental measurements).

⁵²Note that this correction does not take into account electronic relaxations which are obtained upon proper removal of self-interaction effects.